



K23U 1126

Reg. No. :

Name :

IV Semester B.Sc. Degree (CBCSS – OBE – Regular/Supplementary/
Improvement) Examination, April 2023

(2019 Admission Onwards)

CORE COURSE IN MATHEMATICS

4B04 MAT : Number Theory and Applications of Integrals

Time : 3 Hours

Max. Marks : 48

PART – A

Answer **any four** out of five questions. **Each** question carries **1** mark.

1. Define a prime number.
2. State Euclidian lemma.
3. When we can say that the existence of solution Diophantine equation of the form $ax + by = c$?
4. State Wilson's theorem.
5. Show that for any integers a, n , $a \equiv a \pmod{n}$. (4×1=4)

PART – B
(Short Essay Type)

Answer **any eight** out of eleven questions. **Each** question carries **2** marks.

6. If $a|b$, then show that $a|bc$, for any integer c .
7. Find $\gcd(24, 138)$ using Euclidian algorithm.
8. Show that, if p is a prime and $p|ab$, then $p|a$ or $p|b$.
9. If $a \equiv b \pmod{n}$, prove that $\gcd(a, n) = \gcd(b, n)$.

P.T.O.



10. State Fermat's little theorem.
11. Evaluate $\int_{-1}^1 3x^2 \sqrt{x^3 + 1} dx$.
12. Find the area of the region bounded above by $y = x + 6$ bounded below by $y = x^2$, and bounded on the sides by the lines $x = 0$ and $x = 2$.
13. Define volume problem.
14. Find the volume of the solid that is obtained when the region under the curve $y = \sqrt{x}$, over the interval $[1, 4]$ is revolved about x-axis.
15. Find the arc length of the spiral $r = e^{\theta}$ between $\theta = 0$ and $\theta = 2 + \pi$.
16. Find the area of the surface generated by $y = 7x$, $0 \leq x \leq 1$, revolving about x-axis. (8×2=16)

PART – C
(Essay Type)

Answer **any four** out of seven questions. **Each** question carries **4** marks.

17. Solve the Diophantine equation $172x + 20y = 1000$.
18. Express 6 as a linear combination of 12378 and 3054.
19. Find $2^{340} \pmod{341}$.
20. Find the area of the region enclosed by $x = y^2$ and $y = x - 2$.
21. Find the area of the region enclosed by the rose curve $r = \cos 2\theta$.
22. Find the arc length of the curve $y = x^{\frac{3}{2}}$, from $(1,1)$ to $(2, 2\sqrt{2})$.
23. Find the area of the surface that is generated by revolving the portion of the curve $y = x^3$ between $x = 0$ and $x = 1$ about the x-axis. (4×4=16)

PART – D
(Long Essay Type)

Answer **any two** out of four questions. **Each** question carries **6** marks.

24. Let x_0, y_0 is any particular solution of the Diophantine equation of the form $ax + by = c$, then show that all other solutions can be represented by $x = x_0 + \left(\frac{b}{d}\right)t, y = y_0 + \left(\frac{a}{d}\right)t$, where $d = \gcd(a, b)$.
25. Use Euler's theorem, evaluate $2^{100000} \pmod{77}$.
26. Find the area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, using integration.
27. Find the volume of the solid generated when the region under $y = x^2$ over the interval $[0, 2]$ is revolved about the line $y = -1$. **(2×6=12)**
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